

NBER WORKING PAPER SERIES

NEW GOODS AND THE TRANSITION TO A NEW ECONOMY

Jeremy Greenwood
Gokce Uysal

Working Paper 10793
<http://www.nber.org/papers/w10793>

NATIONAL BUREAU OF ECONOMIC RESEARCH
1050 Massachusetts Avenue
Cambridge, MA 02138
September 2004

Updates <http://www.econ.rochester.edu/Faculty/GreenwoodPapers/n2n.pdf>. The views expressed herein are those of the author(s) and not necessarily those of the National Bureau of Economic Research.

©2004 by Jeremy Greenwood and Gokce Uysal. All rights reserved. Short sections of text, not to exceed two paragraphs, may be quoted without explicit permission provided that full credit, including © notice, is given to the source.

New Goods and the Transition to a New Economy
Jeremy Greenwood and Gokce Uysal
NBER Working Paper No. 10793
September 2004
JEL No. E13, O11, O41

ABSTRACT

The U.S. went through a remarkable structural transformation between 1800 and 2000. In 1800 the majority of people worked in agriculture. Barely anyone did by 2000. What caused the rapid demise of agriculture in the economy? The analysis here concentrates on the development of new consumer goods associated with technological progress. The introduction of new goods into the framework lessens the need to rely on satiation points, subsistence levels of consumption, and the like. The analysis suggests that between 1800 and 2000 economic welfare grew by at least 1.5 percent a year, and maybe as much as 10 percent annually, the exact number depending upon the metric preferred.

Jeremy Greenwood
Department of Economics
University of Rochester
P.O. Box 270156
Rochester, NY 14627-0156
and NBER
gree@troi.cc.rochester.edu

Gokce Uysal
Department of Economics
University of Rochester
P.O. Box 270156
Rochester, NY 14627-0156

I. Introduction

A. Facts

In 1800 agriculture accounted for 46 percent of U.S. output, while 74 percent of the U.S. population worked in agriculture. By 2000 agriculture made up 1.4 percent of output. Less than 2.5 percent of the populace worked in agriculture. Figure 1 tells the story about the decline in agriculture.¹ What could have accounted for agriculture's precipitous fall? The idea here is that along with economic development many new goods are introduced. As incomes rise, expenditure gets directed toward new products. That is consumption moves in large measure along the extensive margin, so to speak, and not the intensive one.

New Goods: The number of goods produced has increased dramatically since the Second Industrial Revolution. The increase in the number of consumption goods is hard to document. Historically, home production accounted for a large amount of consumption. For instance, 92 percent of baked goods were made at home in 1900.² This had dropped to 22 percent by 1965. Similarly, 98 percent of vegetables consumed were unprocessed, as opposed to 30 percent in 1970.³ Per-capita consumption of canned fruits rose from 3.6 pounds in 1910 to 21.6 pounds in 1950.⁴ In the early 1970s there were 140 vehicle models available.⁵ This had risen to 260 by the late

¹The data for agriculture's share of income derives from four sources: (i) 1800-1830, Weiss (1994, Tables 1.2, 1.3 and 1.4); (ii) 1840-1900, Gallman (2000, Table 1.14); (iii) 1910-1970, *Historical Statistics of the United States: Colonial Times to 1970* (Series F 251); 1980-2000, Bureau of Economic Analysis, US Department of Commerce. The numbers from Weiss (1994) were obtained by multiplying his series on output per worker by the size of the labor force (prorated by his labor-force participation rate). The data on agriculture's share of employment comes from three sources: (i) 1800 to 1900, Margo (2000, Table 5.3); (ii) 1910 to 1960, Lebergott (1964, Tables A1 and A2); (iii) 1970-1999, U.S. Census Bureau, US Department of Commerce.

²See Lebergott (1976, Table 1, p. 105).

³Ibid.

⁴Ibid.

⁵Federal Reserve Bank of Dallas, 1998 Annual Report, (Exhibit 3, p. 6).

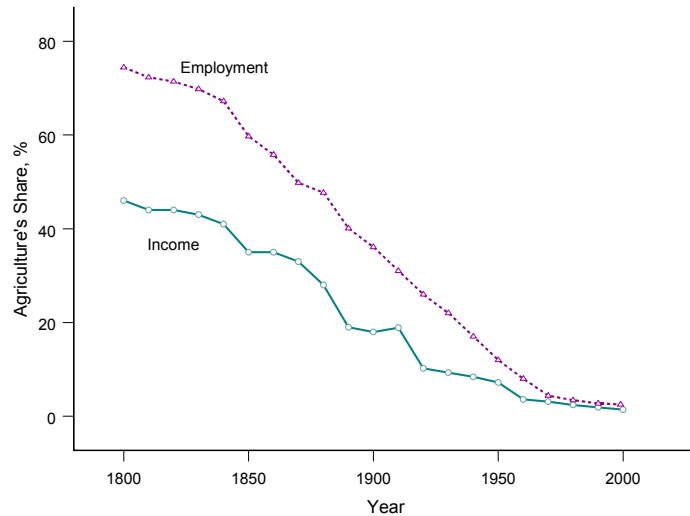


Figure 1: The Decline of Agriculture, 1800-2000.

1990s. Likewise, there were 2,000 packaged food products available in 1980 compared with about 10,800 today.⁶

Trademarks and the Number of Firms: Another measure of the rise in new goods might be trademarks. A trademark is a symbol used by a manufacturer to distinguish his product from others. Figure 2 shows the registration of trademarks since 1870. This is a flow measure. It can be thought of as a proxy for the number of new goods introduced each year. The stock of outstanding trademarks at a point in time will be much larger. It can be estimated using data on trademark registrations and renewals.⁷ Likewise, one might expect that as the number of goods and services

⁶Ibid.

⁷For period 1891 to 1970 the data on registered trademarks and renewals was taken from *Historical Statistics of the United States: Colonial Times to 1970* (Series W 107 and 108). These series were updated using data from the United States Patent and Trademark Office, US Department of Commerce, Annual Reports. The stock of trademarks was computed as follows: Let the time- t stock be denoted by t_t . The stock of trademarks is assumed to evolve in line with

$$t_{t+1} = \delta t_t + [i_t + r_t],$$

in the U.S. economy increases so will the number of firms. There is some evidence suggesting that this is the case. Figure 3 plots the number of firms per capita in the U.S. economy.⁸ As can be seen, it rises.

Consumer Expenditure Patterns: Figure 4 traces some major categories of Personal Consumption Expenditure taken from the National Income and Product Accounts.⁹ At the turn of the last century spending on food accounted for 44 percent of the household budget. Today it is 15 percent. The decline in food's share of total expenditure was matched by a rise in spending in other categories. The only other category showing a secular decline similar to food is clothing. Until recently most other expenditure categories were small relative to food. Spending on medical care, which shows a rapid increase, now exceeds spending on food. Clearly the rise in

where i_t represents new registrations at time t , r_t is renewals, and δ is the depreciation factor on trademarks. Trademarks need to be renewed roughly every 20 years. Most of them aren't. Now, represent the mean of $r_t/(r_{t-20} + i_{t-20})$ by $\overline{r_t/(r_{t-20} + i_{t-20})}$. This measures the survival rate on trademarks. The depreciation factor on trademarks is then taken to be given by

$$\delta = \left[\overline{r_t/(r_{t-20} + i_{t-20})} \right]^{1/20}.$$

⁸This evidence is based on income tax receipts: *Historical Statistics of the United States: Colonial Times to 1970* (Series V1) and the corresponding updated data taken from Internal Revenue Service, U.S. Department of the Treasury. This data encompasses virtually all business in the U.S. and includes corporations, partnerships, and non-farm sole proprietorships. Evidence based on data taken from Dun & Bradshaw, Inc shows that the number of firms per capita has remained constant – *Historical Statistics of the United States: Colonial Times to 1970* (Series V20). The latter series is probably the least preferable and is biased toward large firms. It is based on financial market dealings and excludes many types of business – those engaged in amusements, farming, finance, insurance, one-man services, professions, and real estate. The series for the number of firms was deflated by size of the population as recorded in the *Statistical Abstract of the United States* (2001, Table 1).

⁹Source: National Income and Product Accounts, Personal Consumption Expenditure by Type of Product, Table 2.6, Bureau of Economic Analysis, US Department of Commerce. The numbers for 1900 to 1929 are taken from Lebergott (1996, Table A1).

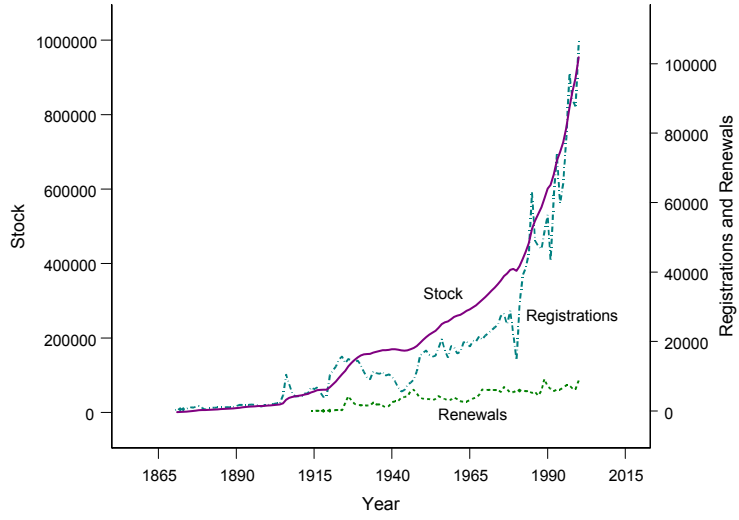


Figure 2: Estimated Stock of Trademarks, 1871-2000.

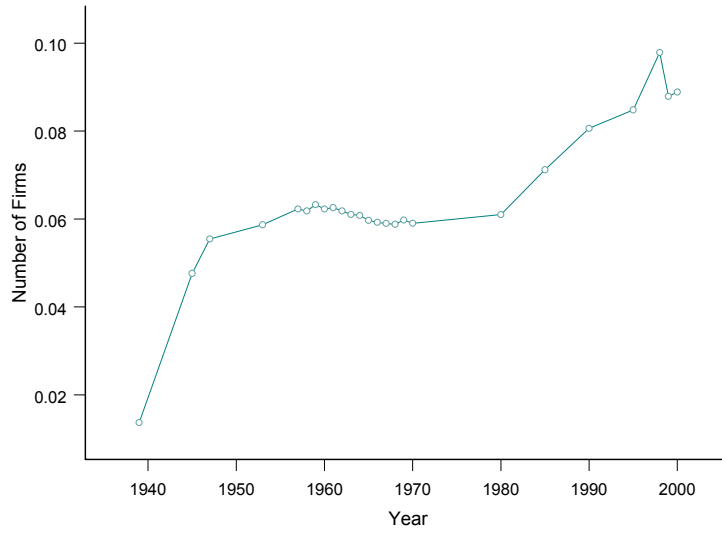


Figure 3: Number of Firms per Capita, 1939-2000.

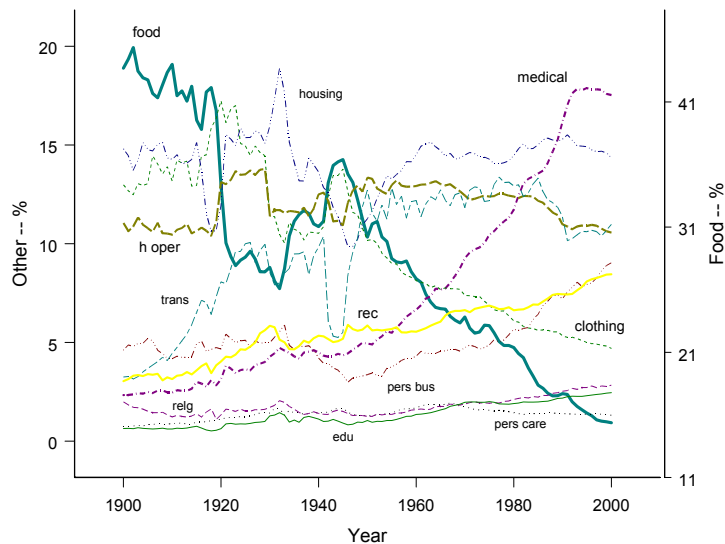


Figure 4: Expenditure Shares by Major Categories, 1900-2000: Purchased Food; Household Operation; Clothing, Accessories and Services; Medical Care; Education; Personal Care; Personal Business; Recreation; Religion and Welfare; Housing; Transportation.

medical spending was associated with the development of new goods. Figure 5 makes this point clear with a chronology of medical innovations. Likewise, Figure 6 plots expenditure on electricity, a component of the near stationary household operations category shown in Figure 4. While electricity is a relatively small fraction of the household budget, it shows a strong upward trend over the last hundred years, linked with the development of many new electrical goods. Last, over the last century total recreation has increased its share in the household budget. Figure 7 shows spending on toys, a component of this category.

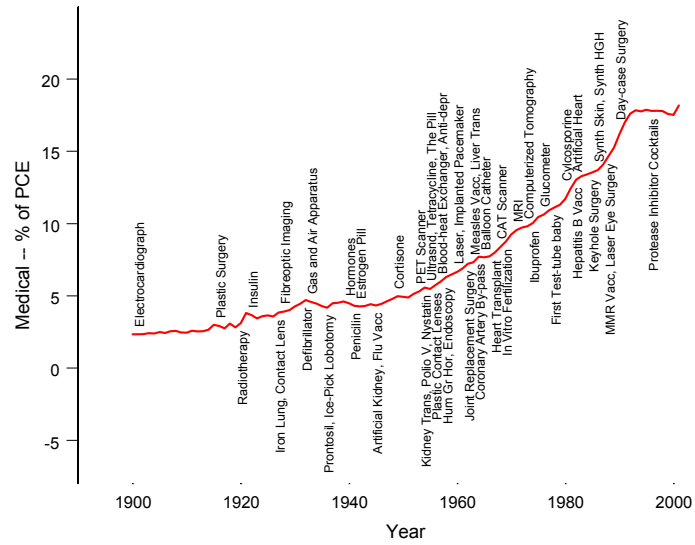


Figure 5: Medicine, 1900-2000.

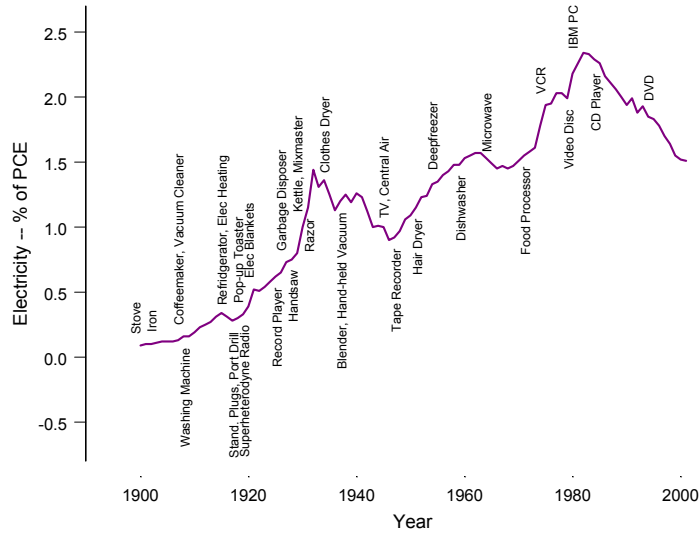


Figure 6: Electricity, 1900-2000.

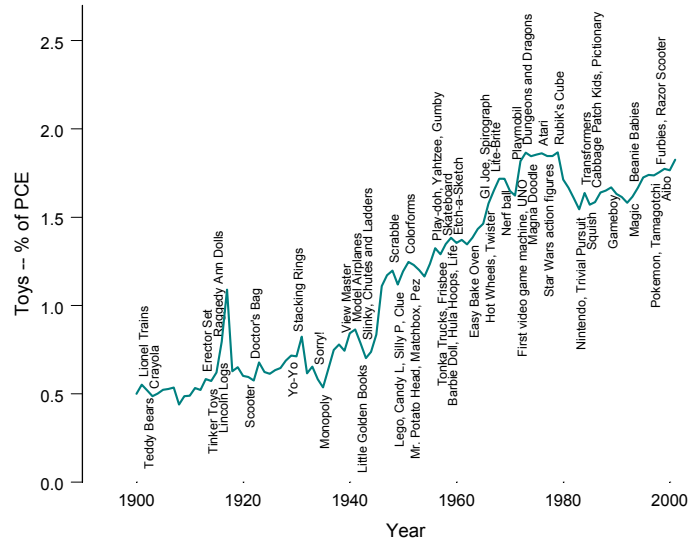


Figure 7: Toys, 1900-2000.

B. The Analysis

Kuznets (1957) was an early researcher to report some facts about agriculture, both across time and space. He documented the secular decline in agriculture's shares of output and employment for a number of countries (see his Tables 7 and 14). He also noted that agriculture declined with economic development in a cross section of countries (see his Tables 3 and 10).

Given these facts some models have been developed that connect structural transformation with economic development. Two first-rate examples are Echevarria (1997) and Laitner (2000). Laitner (2000) develops a model of the decline in agriculture and the rise in manufacturing that occurs with economic progress. His analysis relies on a satiation level for agricultural consumption. At a certain point an increase in agricultural consumption provides no more utility. At this stage individuals start consuming manufacturing goods. Echevarria's (1997) model is quite similar. In her setting the utility function for primary goods (read agricultural goods for the current

purpose) is more concave at low levels of income than are the utility functions for manufacturing and services. Therefore, at low levels of income an individual prefers to spend most of his income on primary goods. A subsistence level for primary goods consumption would work in a similar way. Along these lines, restrictions on tastes and technology that allow for tractable solutions to growth models have been developed by Kongsamut *et al.* (2001). Last, Gollin *et al.* (2002) argue that the release of labor from agriculture, due to gains in productivity, is an important spur in the economic development process.

There is nothing wrong with modelling structural change in this fashion. In fact, it can be viewed as a shorthand for the model built here. The idea here is that at higher levels of economic development it pays to bring new goods on line. This notion is contained in a classic paper by Romer (1987). The application and formulation here are different though: the current analysis focuses on structural change and the analysis is done within the context of a multisector model with perfect competition and *decreasing* returns to scale.¹⁰ With additively separable concave utility, the benefit from bringing a new good on line will exceed the benefit from consuming more of an old good. Thus, the need to rely on satiation and subsistence points in utility can be lessened (or even avoided if desired). Plus, the consumption of a greater array of goods seems to be part and parcel of economic development. The model developed here matches quite well the pattern of structural change observed in

¹⁰In interesting work Yorukoglu (2000) connects the development of new goods with business cycles. In his model firms must decide each period whether or not to attempt to introduce a new product. Once a product is introduced it goes through “process innovation” over time whereby it can be manufactured at lower and lower cost. His setup has interesting implications for economic fluctuations. Suppose the number of products out on the market is small relative to the size of the economy. It will be profitable for firms to attempt to introduce new products. This will lead to a burst of product innovation and a boom. Eventually, the market may become flooded with products. It then no longer pays to introduce a new product. So, product innovation stalls. Worse still, process innovation implies that the existing products can be produced at lower and lower cost. This may lead to a decline in employment. Hence, a recession ensues.

the U.S. data. An interesting question to ask is: By how much has economic welfare increased over the last 200 years? It is easy to address this question through the eyes of the model. The answer obtained is compared with some conventional model-free measures of the rise in living standards.

II. The Model

A. Tastes and Technology

The world is described by a three-sector overlapping-generations model. An individual lives for two periods. The first sector in the economy produces agricultural goods. The second manufactures a generic good, and the last sector produces new goods.

Tastes: Represent the momentary utility function for a person by

$$\alpha \ln(a) + \psi \ln(c) + \sigma \int_{i=0}^N \ln(\max(s_i, \underline{s})) di,$$

$$0 < \alpha, \psi, \sigma < 1 \quad \text{and} \quad \alpha + \psi + \sigma = 1. \quad (1)$$

Here a is the quantity consumed of agricultural goods. Each person also consumes a generic manufacturing good, c , that is produced by the urban sector. The quantity consumed of new good i is denoted by s_i . The term \underline{s} represents a lower bound on new goods consumption. For whatever reason, in the real world there does seem to be some lumpiness in the consumption of goods. This would arise endogenously if there are fixed costs associated with purchasing or consuming a good (or for that matter producing each unit). Without this assumption an individual would unrealistically desire to consume some amount of all goods, so long as prices are finite, albeit perhaps in infinitesimal quantities. With this assumption an individual will want to consume a determinate number of new goods, given a particular set of prices. Additionally,

this assumption permits utility to be defined when some goods aren't consumed.¹¹ The variable N represents the upper bound on the number of new goods that can ever be produced.

Sources and Uses of Income: All individuals supply one unit of labor. They work only when young and earn the wage w . An individual can use his income for consumption or savings. Savings is done using bonds, b , which pay gross interest at rate r . These bonds are backed by capital. Agricultural goods and new goods can be purchased at the prices p_a and p_i .

Production: The output of agricultural goods, y_a , is governed by a standard Cobb-Douglas production function,

$$y_a = z_a k_a^\lambda l_a^{1-\lambda},$$

where k_a and l_a are the quantities of capital and labor hired in agriculture. Likewise y_c units of the generic manufacturing good can be produced using k_c units of capital

¹¹Any properly specified new-goods model must define utility when some new goods aren't consumed. To illustrate the issue, consider a utility function over new goods of the form $\sigma N \ln[(1/N) \int_{i=0}^N s_i^\rho di]^{1/\rho}$, for $\rho \leq 1$. This utility function is often adopted in Romer-style new-goods models. Observe that when $\rho = 0$ one gets a logarithmic utility function of the form employed in (1), ignoring the presence of the lower bound; i.e., when $\max(s_i, \underline{s})$ is replaced by s_i . While this setup may appear to be more general than the one used here, note that for the purposes at hand, this utility function will not be suitable for use when $\rho \leq 0$ – when degree of curvature is greater than or equal to the \ln case. In this situation utility is not well defined when $s_i = 0$ for some i . This is typically finessed by ignoring the zero terms in the utility function. That is, by defining the utility function to be $\sigma N \ln[(1/N) \int_{\mathcal{N}} s_i^\rho di]^{1/\rho}$, for $\rho \leq 1$, where $\mathcal{N} = \{i : s_i > 0\}$. In the logarithmic case this amounts to saying that zero consumption of good s_i yields zero utility. Now, if this is strictly true then no one would consume less than one unit of s_i , since this yields negative utility; i.e., $\ln(s_i) < 0$ when $s_i < 1$. Therefore, this implicitly sets a lower bound on consumption of $\underline{s} = 1$. Hence, when this assumption is explicitly taken into account the analysis proceeds along the lines developed here. Even when $0 < \rho < 1$, $\lim_{s_i \rightarrow 0} d \ln[(1/N) \int_{i=0}^N s_i^\rho di]^{1/\rho} / ds_i = \infty$. This has the unrealistic feature that an individual will consume all goods so long as prices are finite, albeit perhaps some in infinitesimal quantities.

services and l_c units of labor according to

$$y_c = z_c k_c^\omega l_c^{1-\omega}.$$

Output from this sector is used for both consumption and capital accumulation.

Finally, a type- i new good is produced in line with

$$y_i = z_i k_i^\kappa l_i^\tau. \tag{2}$$

There is a fixed cost, ϕ , associated with the production of each new good i . This cost is in terms of labor. The idea is that this fixed cost will slow down the introduction of new goods into the economy.¹² To cover the fixed cost, firms must earn profits after meeting their variable costs. To this end, assume that there are decreasing returns to scale in production. There is free entry into all production activity. The number of specialized firms will be determined by a zero-profit condition. Denote the number of firms that produce the new good i by n_i . Assume that total factor productivity is common across all types of new goods so that $z_i = z_s$ for all $i, s \in [0, N]$.

Capital Accumulation: At a point in time the aggregate stock of capital will be represented by \mathbf{k} . The law of motion for capital is described by

$$\mathbf{k}' = \delta \mathbf{k} + \mathbf{i},$$

where δ is the factor of depreciation and \mathbf{i} represents gross investment (in terms of the generic manufacturing good). There is free mobility of capital across sectors.

Technological Progress: Technological progress will be captured by growth in z_a , z_c , and z_i . As z_i rises it becomes easier to recover the fixed costs associated with producing new goods. As z_a and z_c also rise so does consumer income, and hence the demand for a greater number of new goods. Therefore, the number of new goods produced will increase over time. This leads to a natural decline in agriculture's share of the economy.

¹²This assumption isn't needed for the theory.

B. A Young Worker's Optimization Problem

How will a young worker choose his consumption plan? Given the form of preferences (1), it's clear that if a young worker consumes new good i then he will set $s_i \geq \underline{s}$. Without loss of generality, order the new goods from the lowest to the highest price and assume that a young worker chooses to consume the first I new goods when young, and the first I' when old. A young worker's optimization problem can then be written as

$$\begin{aligned} & \max_{a, a', c, c', s_i \geq \underline{s}, s_i' \geq \underline{s}, I, I'} \{ \alpha \ln(a) + \psi \ln(c) + \beta \alpha \ln(a') + \beta \psi \ln(c') \\ & + \sigma \int_{i=0}^I \ln(s_i) di + \beta \sigma \int_{i=0}^{I'} \ln(s_i') di + \sigma(N - I) \ln(\underline{s}) + \beta \sigma(N - I') \ln(\underline{s}) \}, \end{aligned} \quad (3)$$

subject to

$$c + p_a a + \frac{c'}{r'} + \frac{p'_a a'}{r'} + \int_{i=0}^I p_i s_i di + \int_{i=0}^{I'} \frac{p'_i s_i'}{r'} di = w. \quad (4)$$

Here the superscript “o” denotes an allocation when old while the “y” signifies that a variable's value next period is being considered. This problem is more or less standard with one twist: the determination of the number of new goods to consume.

The Consumption of Each Good: Given logarithmic structure for preferences, it is easy to solve for the quantity consumed of each good. The solution for c is given by

$$c = \frac{\psi}{\alpha + \psi + \beta \alpha + \beta \psi + \sigma I + \beta \sigma I'} w. \quad (5)$$

Likewise, the solutions for s_i and s_i' read

$$p_i s_i = \frac{\sigma}{\alpha + \psi + \beta \alpha + \beta \psi + \sigma I + \beta \sigma I'} w, \quad (6)$$

and

$$\frac{p'_i s_i'}{r'} = \frac{\beta \sigma}{\alpha + \psi + \beta \alpha + \beta \psi + \sigma I + \beta \sigma I'} w, \quad (7)$$

at least when $s_i > \underline{s}$ and $s_i' > \underline{s}$. In the equilibrium being developed all new goods will sell at the same price, p_s , so that $p_i = p_s$ for all i . Hence, $s_i = s_s$ for all i such that $s_i > \underline{s}$; likewise, $s_i' = s_s'$ for all i such that $s_i' > \underline{s}$.

The Number of New Goods: The first-order conditions for the number of new goods consumed each period, I and I' , are given by

$$\sigma[\ln(s_I) - \ln(\underline{s})] \leq \frac{\psi}{c} p_I s_I \text{ (with equality if } I > 0), \quad (8)$$

and

$$\beta\sigma[\ln(s'_{I'}) - \ln(\underline{s})] \leq \frac{\psi}{c} p'_{I'} \frac{s'_{I'}}{r'} \text{ (with equality if } I' > 0). \quad (9)$$

Take expression (8). The value of an extra good is $\sigma[\ln(s_I) - \ln(\underline{s})]$, the lefthand side. This good costs $p_I s_I$. To convert this cost into utility terms multiply by the marginal utility of first-period consumption or ψ/c to get $\psi p_I s_I/c$, the righthand side. Using (5), (6) and (7) it conveniently follows that¹³

$$s_I = s'_{I'} = e\underline{s}. \quad (10)$$

Now, when will (8) and (9) hold with strict equality? It is easy to deduce that both equations can hold tightly only when $p_I = p'_{I'}/(r'\beta)$. If $p_I < p'_{I'}/(r'\beta)$ then

¹³Observe that as the lower bound \underline{s} approaches zero the quantity of new good I consumed, s_I , becomes infinitesimal. That is, as \underline{s} falls the individual would like to consume more new goods by consuming less of each new good. Without a lower bound on consumption, \underline{s} , the individual would like to consume the whole spectrum of new goods, albeit in infinitesimal quantities as N becomes large. This is true in a Romer-style model, too. In the current setting with perfect competition, as \underline{s} declines the number of firms producing each new good will decline. In Romer (1987) this is precluded by the monopoly assumption that restricts the number of firms producing each good to be one. This limits the total number of goods that can be produced.

The feature that a consumer would like to consume all goods when prices are finite, although perhaps in infinitesimal quantities, is unrealistic. The lower bound on consumption, \underline{s} , avoids this problem. Another way to proceed, might be to use a utility function over new goods of the form $\int_{i=0}^N U(s_i) di$, with $-M < U(0), U_1(0) < M$ for some $M > 0$. Here utility is well defined when a new good isn't consumed. And, at a high enough price the individual will choose not to consume a good. This is not in the class of utility functions typically used in applied work, though. Note that parts of the current analysis will still carry through. For instance, the equation (8) determining the number of new goods will appear as $U(s_I) - U(0) = (\psi/c)p_I s_I$ (with equality if $I > 0$). The intuition for this equation is identical to (8).

only (8) can hold. In this situation it is optimal to consume new goods just when young so that $I' = 0$. To summarize:

$$\begin{aligned}
I \geq 0 \text{ and } I' = 0, & \quad \text{if } p_I < p'_{I'}/(r'\beta), \\
I \geq 0 \text{ and } I' \geq 0, & \quad \text{if } p_I = p'_{I'}/(r'\beta), \\
I = 0 \text{ and } I' \geq 0, & \quad \text{if } p_I > p'_{I'}/(r'\beta).
\end{aligned} \tag{11}$$

In the subsequent analysis only the first two cases transpire. These two cases will be referred to as Zone 1 and Zone 2.

Discussion: Some intuition for the solution to the consumer's problem (3) can be gleaned from Figure 8.¹⁴ For expositional purposes, assume that the economy is in Zone 1 and let all new goods sell at the same price p_i – again, an assumption that will be met in equilibrium under study. Now, consider the decision to consume the marginal new good, I . How much of new good I should the agent purchase: $s_I = 0$, which amounts to not consuming, or some quantity $s_I \geq \underline{s}$? The utility that an agent derives from consuming more of new good I is shown on the diagram. If the consumer doesn't buy I he realizes the utility level $\ln(\underline{s})$, indicated by the rectangle. Alternatively, if he buys the good then he will purchase more than \underline{s} and experience the utility level $\ln(s_I)$. Utility then rises in the fashion shown by the concave utility function UU' . The cost of consuming new good I is shown by the straight line CC' . First, by consuming I the agent loses the automatic utility level $\ln(\underline{s})$, so to speak, associated with not consuming it – cf. (3). Second, by buying more of new good I the agent diverts expenditure away from consuming more of the other new goods. These goods cost the same as I and have a marginal utility of $1/s_i = 1/(e\underline{s})$, the slope of the line CC' . The individual will pick the consumption quantity, s_I , that equates marginal benefit and marginal cost. This will be the level associated with the point of tangency between the two lines (as shown by the inverted triangle). Here, $\ln(s_I) = \ln(\underline{s}) + s_I/(e\underline{s})$, which implies $s_I = e\underline{s} - \text{c.f. (8) in conjunction with (5) and (6)}$.¹⁵

¹⁴Credit for this diagram goes to Shouyong Shi.

¹⁵The solution to consumer's problem has a similarity to employment lotteries, à la Rogerson

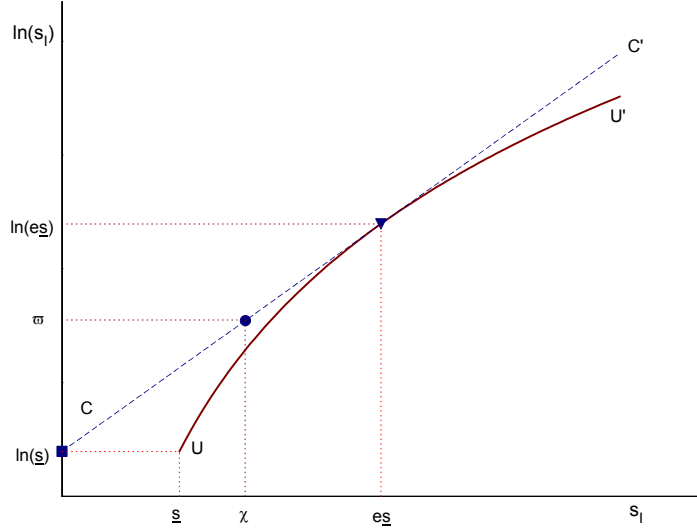


Figure 8: The determination of s_I .

(1988). There is a nonconvex region in preferences, as Figure 8 clearly shows. The individual convexifies this by moving along extensive margin. He consumes some new goods, and not others. In the equilibrium under study, for each new good $i \in [0, N]$ the individual can be thought of choosing the quantity s_i from the two-point set $\{0, e\u0302_s\}$. He randomly picks some new goods on the $[0, N]$ -spectrum to maximize his utility. Let him choose to consume the fraction I/N of new goods when young, and the fraction I'/N when old. His decision problem can be formulated as

$$\begin{aligned} & \max_{a, a^{o'}, c, c^{o'}, I/N, I'/N} \{ \alpha \ln(a) + \psi \ln(c) + \beta \alpha \ln(a^{o'}) + \beta \psi \ln(c^{o'}) \\ & + \sigma N \left[\frac{I}{N} \ln(e\u0302_s) + \left(1 - \frac{I}{N}\right) \ln(\underline{s}) \right] + \beta \sigma N \left[\frac{I'}{N} \ln(e\u0302_s) + \beta \sigma \left(1 - \frac{I'}{N}\right) \ln(\underline{s}) \right] \}, \end{aligned}$$

subject to

$$c + p_a a + \frac{c^{o'}}{r'} + \frac{p'_a a^{o'}}{r'} + \frac{I}{N} N p_i(e\u0302_s) + \frac{I'}{N} N \frac{p'_i}{r'}(e\u0302_s) = w.$$

The solution to this problem is represented by the circle on Figure 8. Here, the individual can be thought of as realizing the level of utility $\varpi = [(I/N) \ln(e\u0302_s) + (1 - I/N) \ln(\underline{s})]$ that is associated with consuming the convex combination of new goods $\chi = (I/N) \times (e\u0302_s) + (1 - I/N) \times 0$.

C. The Firms' Problems

First consider the firm in the generic manufacturing sector. Its problem is

$$\pi_c = \max_{l_c, k_c} [z_c k_c^\omega l_c^{1-\omega} - w l_c - (r - \delta) k_c]. \quad (12)$$

Next, the problem facing a firm in the agricultural sector can be written as

$$\pi_a = \max_{l_a, k_a} [p_a z_a k_a^\lambda l_a^{1-\lambda} - w l_a - (r - \delta) k_a]. \quad (13)$$

Perfect competition implies that factors will be paid their marginal products. Euler's theorem then guarantees that $\pi_c = \pi_a = 0$. From the solution to problem (12), it is easy to deduce that the wage rate can be expressed as a function of the return on capital and the level of TFP in the generic manufacturing sector. The solution to problem (13) then implies that the price of agricultural goods can be expressed as a function of the return on capital, and the levels of TFP in the agricultural and manufacturing goods sector. Hence, write $w = W(r - \delta; z_c)$ and $p_a = P_a(r - \delta; z_a, z_c)$.¹⁶

Finally, turn to the production of new goods. The problem here is

$$\pi_i = \max_{l_i, k_i} [p_i z_i k_i^\kappa l_i^\tau - w l_i - w \phi - (r - \delta) k_i]. \quad (14)$$

Now, free entry into the production of new goods guarantees that profits will be zero. Therefore,

$$\pi_i = 0. \quad (15)$$

The zero-profit condition in conjunction with the solution to the firm's problem allows for the price of new goods to be expressed as a function of the return on capital, the real wage rate, and the level of TFP. One can therefore write $p_i = P_i(r - \delta; z_c, z_i)$.¹⁷ Since $z_i = z_s$ for all $i, s \in [0, N]$ and P_i is not a function of i , it transpires that $p_i = p_s$ for all i and s that are produced. Note that there is really just one price to worry about, r .

¹⁶The interested reader is referred to equations (21) and (28) in the Appendix.

¹⁷For more detail, see equation (22) in the Appendix.

D. Market-Clearing Conditions

The markets for goods and factors must clear each period. Take the goods markets first. The market-clearing condition for generic manufacturing is

$$c + c^o + \mathbf{k}' - \delta \mathbf{k} = y_c, \quad (16)$$

while the one for agriculture appears as

$$a + a^o = y_a.$$

The market for each new good requires that

$$\mu_i s_i + \mu_i^o s_i^o = n_i y_i,$$

where μ_i denotes the fraction of a generation that will consume good i . Note that in order to have a symmetric equilibrium, the demand must be same for each new good produced. Now, the total number of new goods produced in a period is given by $\max(I, I^o)$. The young generation consumes the fraction $0 \leq I / \max(I, I^o) \leq 1$ of these goods. If each young worker randomly picks his I goods from the $\max(I, I^o)$ being offered then $\mu_i = I / \max(I, I^o)$.¹⁸ Similarly, $\mu_i^o = I^o / \max(I, I^o)$. Now, suppose that $p_i < p'_i / (r'\beta)$; i.e., that the economy is in Zone 1. Then, $\mu_i = 1$ and $\mu_i^o = 0$. Alternatively, if $p_i = p'_i / (r'\beta)$ it may transpire that $0 < \mu_i, \mu_i^o < 1$.

The factor market conditions appear as

$$k_a + k_c + \max(I, I^o) n_i k_i = \mathbf{k},$$

and

$$l_a + l_c + \max(I, I^o) n_i l_i + \max(I, I^o) n_i \phi = 1. \quad (17)$$

¹⁸In other words think about the index i in (3) as representing each young worker's personal numbering scheme over the new goods available in the first and second periods of his life. That is, out of the $\max(I, I^o)$ new goods available in the first period of his life he can choose to order them as he wishes on the interval $[0, \max(I, I^o)]$. The same is true for the second period.

Definition A competitive equilibrium is a set of time paths for consumption, $\{a_t, a_t^o, c_t, c_t^o, s_{i,t}, s_{i,t}^o, I_t, I_t^o\}_{t=0}^\infty$, labor and capital inputs, $\{l_{a,t}, l_{c,t}, l_{i,t}\}_{t=0}^\infty$ and $\{k_{a,t}, k_{c,t}, k_{i,t}\}_{t=0}^\infty$, the number of firms producing new goods, $\{n_{i,t}\}_{t=0}^\infty$, and interest rates, $\{r_t\}_{t=0}^\infty$, such that for an initial capital stock, k_0 , a time path for total factor productivities, $\{z_{a,t}, z_{c,t}, z_{i,t}\}_{t=0}^\infty$, and the pricing functions, $W(\cdot)$, $P_a(\cdot)$, $P_i(\cdot)$:

1. The consumption allocations, $\{a_t, a_{t+1}^o, c_t, c_{t+1}^o, s_{i,t}, s_{i,t+1}^o, I_t, I_{t+1}^o\}_{t=0}^\infty$, solve the consumer's problem (3), given the path for prices $\{W(r_t - \delta; z_{c,t}), P_a(r_t - \delta; z_{a,t}, z_{c,t}), P_i(r_t - \delta; z_{c,t}, z_{i,t}), r_t\}_{t=0}^\infty$.
2. The factor allocations, $\{l_{a,t}, l_{c,t}, l_{i,t}\}_{t=0}^\infty$ and $\{k_{a,t}, k_{c,t}, k_{i,t}\}_{t=0}^\infty$, solve the firms' problems (12) to (14), given the path for prices $\{W(r_t - \delta; z_{c,t}), P_a(r_t - \delta; z_{a,t}, z_{c,t}), P_i(r_t - \delta; z_{c,t}, z_{i,t}), r_t\}_{t=0}^\infty$.
3. There are zero profits in the new goods markets as dictated by (15).
4. All goods and factor markets clear so that equations (16) to (17) hold.

III. Results

Can the above framework explain the rise of manufacturing and the decline of agriculture that occurred over the last two hundred years? The engine of change in the model is technological progress. Hence, to answer this question, some discussion on the extent of technological progress in agriculture and manufacturing over the 1800-to-2000 period of interest is in order.

A. Technological Progress in Agriculture and Non-Agriculture

Take agriculture first. Total factor productivity (TFP) grew at 0.48 percent per year between 1800 and 1900.¹⁹ Its annual growth rate fell to 0.26 percent in the

¹⁹The estimates for the growth rates of agricultural productivity from 1800 to 1900 come from Atack *et al.* (2000, Table 6.1).

interval 1900 to 1929 and then rose to 2.24 percent over the 1929-to-1960 period.²⁰ Between 1960 and 1996 it grew at an annual rate of 2.18 percent.²¹ Hence, by chaining these estimates together, it is easy to calculate that TFP increased by a factor of 7.61 between 1800 and 1996. TFP in the non-agricultural sector – labelled manufacturing – rose at a faster clip. It grew at an annual rate of 0.75 percent over the period 1800 to 1900.²² Its growth rate then picked up to 1.63 percent across 1899 to 1929 and to 2.01 percent from 1929 to 1966.²³ Last, manufacturing TFP grew at an annual rate of 0.70 percent from 1966 to 2000.²⁴ Over the period 1800 to 2000 non-agricultural TFP grew by a factor of 9.25. Figure 9 shows the series obtained for agricultural and non-agricultural TFP.

B. Analysis of Comparative Steady States

Choice of Parameter Values: In order to simulate the model values must be assigned to various parameters. These are listed in Table 1. Almost nothing is known about the appropriate values for some parameters, such as the lower bound on new goods consumption, \underline{s} , or the fixed cost associated with running a firm producing new goods, ϕ . So, the parameter values are picked to generate two steady-state

²⁰The estimates for the growth in agricultural TFP for the 1900-to-1929 and 1929-to-1960 periods are computed from data in *Historical Statistics of the United States: Colonial Times to 1970* (Series W7).

²¹Source: Economic Research Service, United States Department of Agriculture, Agricultural Productivity in the U.S. (98003). Available online at <http://usda.mannlib.cornell.edu/usda/usda.html>.

²²The estimates for technological progress in the nonagricultural sector prior to 1900 are backed out using economy-wide TFP and sectoral share data taken from Weiss (1994, Tables 1.2 -1.4) and Gallman (2000, Tables 1.7 and 1.14) in conjunction with the Atack *et al* (2000, Table 6.1) agricultural estimates.

²³These estimates are calculated from data in *Historical Statistics of the United States: Colonial Times to 1970* (Series W8).

²⁴Source: Bureau of Labor Statistics, U.S. Department of Labor, Multifactor Productivity Trends, Table 2: Private Non-Farm Business: Productivity and Related Indexes, 1948-2001. Available on line at <http://www.bls.gov/news.release/prod3.t02.htm>.

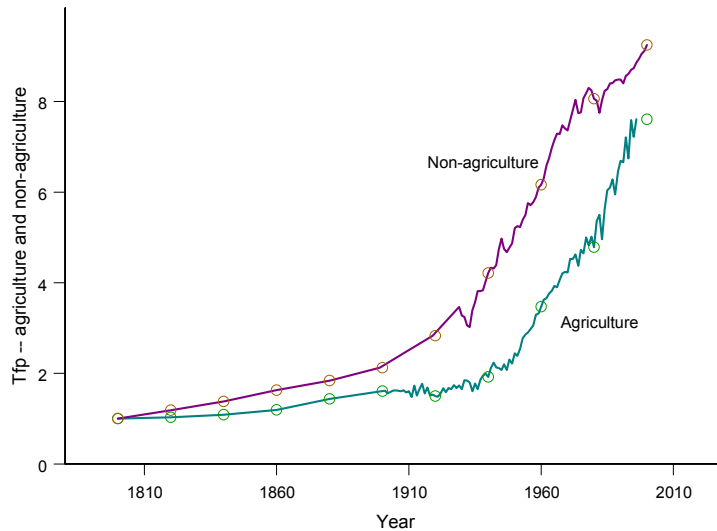


Figure 9: Total factor productivity in agriculture and non-agriculture, 1800-2000.

equilibriums that mimic some key features of the U.S. data for the years 1800 and 2000. A guide to the informal selection procedure adopted will now be given. Before proceeding, assume that a model period is 20 years and that the (annualized) rate of physical depreciation on capital is 8 percent.

U.S. Economy, circa 1800: In 1800 agriculture accounted for 46 percent of U.S. output and 74 percent of employment. A steady state will be constructed that matches these two features. To this end, normalize the initial levels of total factor productivity so that $z_a = z_c = z_i = 1$. Next, assume that no new goods were produced in 1800. This can be achieved by picking high values for \underline{s} and ϕ . By doing this output will be comprised by just agricultural and generic manufacturing goods. While it's hard to know what are reasonable values for labor's share of income in agriculture, $1 - \lambda$, and generic manufacturing, $1 - \omega$, it is known that for the aggregate economy it should be about 70 percent. This implies that

$$\chi(1 - \lambda) + (1 - \chi)(1 - \omega) = 0.70,$$

where χ is agriculture's share of output. This restriction can be used to pin down a value for capital's share in agriculture, λ , given a value for capital's share in the generic manufacturing, ω . In other words, let

$$\lambda = 1.0 + [(1 - \chi_{1800})/\chi_{1800}](1 - \omega) - 0.70/\chi_{1800}.$$

The choice of ω will be discussed shortly.

U.S. Economy, circa 2000: Two hundred years later agricultural's share of output and employment had dropped to just 1.4 and 2.5 percent, respectively. Output had increased by 36.7 times.²⁵ Can a steady state be constructed that replicates these two facts? Over this time period total factor productivity in agriculture rose 7.61 fold. So, set $z_a = 7.61$. Similarly, total factor productivity in non-agriculture increased 9.25 times. Thus, let $z_c = z_i = 9.25$. The responsiveness of output to changes in TFP is sensitive to capital's share of income. The larger capital's share of income is the bigger will be the response. This transpires because capital is the reproducible factor in the model. The observed 36.7-fold increase in output can be obtained by setting capital's share in the generic goods sector, ω , to 0.46. New goods are produced competitively. Therefore, any profits earned in this sector are absorbed completely by the fixed costs of production. Recall that the fixed cost of producing new goods are borne entirely in terms of labor. Thus, labor's share of income in the new goods sector is given by $(1 - \kappa)$. Assuming that new goods weigh heavily in the 2000 economy, this dictates setting κ at about 30 percent; let $\kappa = 0.28$. To choose the exponent on labor, τ , assume that profits, and hence fixed costs, amount to 10 percent of new goods production so that $\tau = 1.0 - \kappa - 0.10$.

Last, three taste parameters need to be picked: α , ψ , and β . In the adopted parameterization the circa-2000 steady state lies in Zone 2. Hence, $r = 1/\beta$.²⁶ An annual interest rate of about 7.5 percent can be achieved by setting $\beta = 0.93$ ²⁰. The weights on the various categories of consumption in utility are chosen to obtain the

²⁵This estimate is based on the data presented in Mitchell (1998, Table J1) together with the NIPA accounts.

²⁶This normally wouldn't be the case for an overlapping generations model.

best fit matching agricultural's share of output and employment over the period 1800 to 2000.

TABLE 1 – PARAMETER VALUES

Tastes: $\alpha = 0.23$, $\psi = 0.22$, $\beta = 0.93^{20}$, $\sigma = 1.0 - 0.23 - 0.22$, $\underline{s} = 0.1$.

Technology: $\omega = 0.46$, $\lambda = 0.11$, $\kappa = 0.28$, $\tau = 0.62$, $\phi = 0.03$, and $\delta = (1.0 - 0.08)^{20}$.

1. Welfare Gain

So by how much did welfare increase between 1800 and 2000? To address this question, define the expenditure function, $E(p_a, p'_a, \vec{p}_i, \vec{p}'_i, r', u)$, by

$$E(p_a, p'_a, \vec{p}_i, \vec{p}'_i, r', u) \equiv \min_{c, c^{o'}, a, a^{o'}, s_i \geq \underline{s}, s_i^{o'} \geq \underline{s}, I, I^{o'}} \left\{ c + p_a a + \frac{c^{o'}}{r'} + \frac{p'_a a^{o'}}{r'} + \int_{i=0}^I p_i s_i di + \int_{i=0}^{I^{o'}} \frac{p'_i}{r'} s_i^{o'} di \right\} \quad (18)$$

subject to

$$\begin{aligned} & \{ \alpha \ln(a) + \psi \ln(c) + \sigma \int_{i=0}^I \ln(s_i) di \\ & \quad + \beta [\alpha \ln(a^{o'}) + \psi \ln(c^{o'}) + \sigma \int_{i=0}^{I^{o'}} \ln(s_i^{o'}) di] \\ & \quad + \sigma(N - I) \ln(\underline{s}) - \beta \sigma(N - I^{o'}) \ln(\underline{s}) \} = u, \end{aligned} \quad (19)$$

where \vec{p}_i represents the vector of new goods prices for the current period. The solution to this problem will be once again characterized by the first-order conditions (5) to (9), but now the choice variables must also satisfy the utility constraint (19) rather than the budget constraint (4).

Consider comparing welfare across two steady states, labeled old and new. Let the subscript 0 denote a variable's value in the old steady state and the subscript T represent the variable's value in the new steady state. In the new steady state a young agent will earn w_T , face the prices $p_{a,T}$, $\vec{p}_{i,T}$, and r_T , and realize utility, u_T . In

the old steady state, the young agent would have earned w_0 and realized utility u_0 . Now, it would cost the amount $E(p_{a,T}, p_{a,T}, \overrightarrow{p_{i,T}}, \overrightarrow{p_{i,T}}, r_T, u_0)$ to provide the old level of utility, u_0 , at the new set of prices, $p_{a,T}$, $\overrightarrow{p_{i,T}}$, and r_T . At this level of income a young agent would be indifferent between living in the new steady state or staying in the old steady one with the wage rate, w_0 . Any extra income improves the agent's lot. Hence, a measure of the proportionate change in welfare across these two steady states, analogous to a compensating variation, is given by²⁷

$$\ln(w_T) - \ln[E(p_{a,T}, p_{a,T}, \overrightarrow{p_{i,T}}, \overrightarrow{p_{i,T}}, r_T, u_0)].$$

Another utility-based measure is based on the concept of an equivalent variation. It measures the cost of providing the new level of utility, u_T , at the prices that the agent faces in old steady-state, $p_{a,0}$, $\overrightarrow{p_{i,0}}$, and r_0 .²⁸ This gives

$$\ln[E(p_{a,0}, p_{a,0}, \overrightarrow{p_{i,0}}, \overrightarrow{p_{i,0}}, r_0, u_T)] - \ln[w_0].$$

Wages increase from w_0 to w_T across the two steady states. This doesn't take into account the fact that the cost of living may have also shifted due to a change in prices. The conventional way to control for this would be to deflate wages in the new steady state by a price index. The Laspeyres price index, L_T , is given by

$$L_T = \frac{(c_0 + c_0^o) + p_{a,T}(a_0 + a_0^o) + p_{i,T}(I_0 + I_0^o)e_{\underline{S}}}{(c_0 + c_0^o) + p_{a,0}(a_0 + a_0^o) + p_{i,0}(I_0 + I_0^o)e_{\underline{S}}}.$$

It measures the rise in the cost of purchasing the initial basket of goods. The growth in real income based on the Laspeyres price index is

$$\ln(w_T/L_T) - \ln(w_0) = \ln(w_T) - \ln(L_T w_0).$$

Of course agents wouldn't buy the initial basket of goods in the new steady state. They would substitute toward those goods whose prices have fallen. The Paasche price

²⁷The compensating variation, CV , associated with the move from the old to the new steady state is $E(p_{a,T}, p_{a,T}, \overrightarrow{p_{i,T}}, \overrightarrow{p_{i,T}}, r_T, u_0) - w_0$. Therefore, definitionally, $E(p_{a,T}, p_{a,T}, \overrightarrow{p_{i,T}}, \overrightarrow{p_{i,T}}, r_T, u_0) = CV + w_0$. Hence, the above welfare measure can be written as $\ln(w_T) - \ln(CV + w_0)$.

²⁸The price vector, $\overrightarrow{p_{i,0}}$, is defined only over the new goods that are in existence in the old steady state.

index, P_T , computes the rise in cost of living using the basket of goods consumed in the final steady state.

$$P_T = \frac{(c_T + c_T^o) + p_{a,T}(a_T + a_T^o) + p_{i,T}(I_T + I_T^o)e_{\underline{s}}}{(c_T + c_T^o) + p_{a,0}(a_T + a_T^o) + p_{i,0}(I_T + I_T^o)e_{\underline{s}}}.$$

The growth in real income using the Paasche price index is

$$\ln(w_T/P_T) - \ln(w_0).$$

The Fisher price index, F_T , is a geometric mean of the Laspeyres and Paasche indices so that $F_T = \sqrt{L_T \times P_T}$. Last, the Tornqvist index, T_T , is defined by

$$\ln(T_T) = \left(\frac{\xi_{a,0} + \xi_{a,T}}{2}\right) \ln\left(\frac{p_{a,T}}{p_{a,0}}\right) + \left(\frac{\xi_{i,0} + \xi_{i,T}}{2}\right) \ln\left(\frac{p_{i,T}}{p_{i,0}}\right),$$

where $\xi_{x,t}$ is the period- t expenditure share of good x (for $x = a, i$) in consumption so that, for example,

$$\xi_{a,0} = \frac{p_{a,0}(a_0 + a_0^o)}{(c_0 + c_0^o) + p_{a,0}(a_0 + a_0^o) + p_{i,0}(I_0 + I_0^o)e_{\underline{s}}}.$$

A problem with the Paasche price index is that many of the goods purchased in the new steady state were not available in the old steady one. For example, assume that no new goods were produced in the old steady state. The price $p_{i,0}$ would not exist then. For this reason, the Laspeyres index is used in practice – the price $p_{i,0}$ won't appear in the denominator of this index since $I_0 = I_0^o = 0$ when new goods aren't consumed. Hicks (1940) suggested constructing a "virtual price" to overcome this problem with new goods. The virtual price is the lowest price for the new good at which the consumer would choose zero units, given the prices for the other goods and his income. It is easy to construct such virtual prices in the model. To see this, assume that no new goods are consumed in the old steady state. Also suppose that $r_0 < 1/\beta$, or that the old steady state lies in Zone 1 (implying in general that $I_0 \geq 0$ and $I_0^o = 0$). Recall that if some new goods are consumed then equation (8) will hold with equality so that $s_i = e_{\underline{s}}$. Therefore, using (6) it will transpire that

$$p_{i,0} = \frac{\sigma}{\alpha + \psi + \beta\alpha + \beta\psi + \sigma I_0} \frac{w_0}{e_{\underline{s}}}.$$

This equation gives the inverse demand curve for new goods. To compute the virtual price, $p_{i,0}^v$, set $I_0 = 0$ in this demand relationship to obtain

$$p_{i,0}^v = \frac{\sigma}{\alpha + \psi + \beta\alpha + \beta\psi} \frac{w_0}{e\underline{s}}.$$

Some intuition for the differences between the various welfare measures is provided in Figure 10. The diagram portrays a static setting with just two types of goods, generic and new. Tastes are once again represented by (3), but now set $\alpha = \beta = 0$. Equation (10) will once again give the quantity consumed of each new good, or $s_i = e\underline{s}$. Given this, Figure 10 shows indifference curves over the quantity of generic goods, c , and the number of new goods, I , consumed. The slope of one of these indifference curves is $-\psi/(\sigma c)$. Now, imagine a situation where there are no new goods produced. Here $c = w$. This situation is portrayed by the point A . Suppose that new goods become available. Point B shows this situation. Recall that in equilibrium each new good that is produced will sell at the same price, p_i . The slope of the budget constraint is given by $-1/(p_i e\underline{s})$ – the cost of consuming $e\underline{s}$ units of a new good is $p_i e\underline{s}$.²⁹ Clearly the consumer is better off. He is on a higher indifference curve. At the new prices, you could take away from the consumer CV units of income and he would remain on his old indifference curve at the point D . This shows the compensating variation. The Laspeyres price index shows no change in real income. Why? At the new set of prices the cost of the old consumption bundle is still w since *no* new goods were consumed. Hick’s (1940) virtual price is given by slope of the indifference going through the point A . According to the Paasche index real income increases by the amount P . By giving the consumer this amount he can afford to buy the new bundle of goods, represented by point B , at the old set of (virtual) prices. Last, the distance EV measures the equivalent variation. It asks how much income would consumer have to be given in order to get his new level of utility without any new goods – see point E .

Table 2 presents the gain in welfare according to the various measures. The

²⁹The budget constraint is $c + p_i I e\underline{s} = w$.

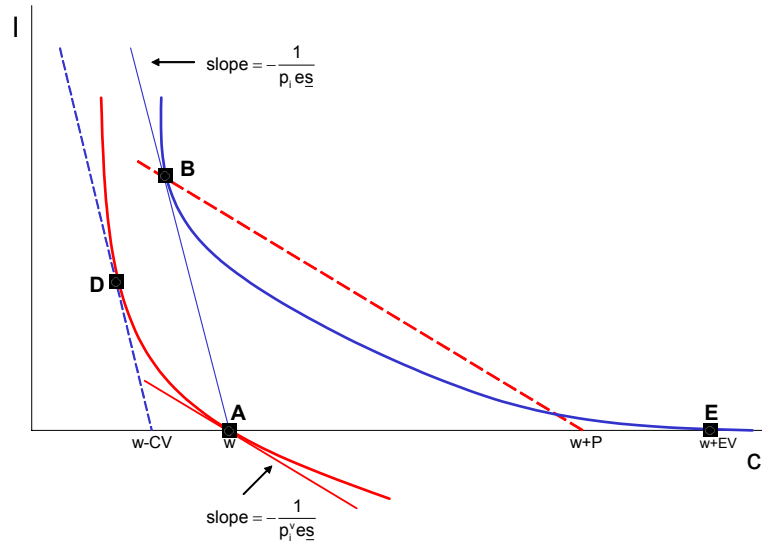


Figure 10: Welfare Measures.

welfare gain due to technological progress and the introduction of new goods is large by any measure. The utility-based estimate based upon the compensating variation suggests that welfare rose by 300 percent, when measured in terms of generic consumption. This is a (continuously compounded) gain of about 1.5 percent a year. The traditional index number measures report gains very similar to the compensating variation criteria. These numbers are strikingly similar to an estimated 300 percent increase in the U.S. real wage over the 1800 to 2000 period.³⁰ The other utility-based estimate based upon equivalent variation concept reports a much larger welfare gain of 2,000 percent. This translates into a welfare gain of about 10 percent a year. This measure asks by how much would income have to increase in 1800, when there were no new goods, in order to provide today's level of utility. Providing a modern utility level using just yesteryear's goods is an expensive proposition. The traditional index

³⁰This estimate is based on real wage data contained in Williamson (1995, Table A1) for the period 1830 to 1988. The Williamson (1995) series was updated to 2000 using data from the Bureau of Labor Statistics. The resulting series was then extrapolated back to 1800.

number concepts miss this point. Theoretically speaking, there is no good reason to prefer the compensating over the equivalent variation, or vice versa. Taking an average of the two utility-based measures suggests that welfare increased by 1,151 percent or grew at about 6 percent a year. Perhaps the safest thing to say, though, is that welfare increased by at least 300 percent.

TABLE 2: GAIN IN WELFARE

<i>Measure</i>	<i>Welfare Gain, %</i>
Compensating Variation	309
Equivalent Variation	1,994
Laspeyres	280
Paasche	305
Fisher	292
Tornqvist	302

C. Transitional Dynamics

The Computational Experiment: Now, imagine starting the model off in a steady state that resembles the U.S. in 1800 and letting it converge to a new steady state that resembles the U.S. in 2000. To undertake this experiment the time path for TFP shown in Figure 9 will be inputted into the simulation. The circles on the series indicate the values at 20 year intervals that will be used when simulating the model's transitional dynamics. What will the economy's behavior over this time period look like? From the earlier results it can be surmised that economy will initially be in Zone 1 and then transit into Zone 2. So before proceeding, a comment will be made about the model's local dynamics in Zone 2.³¹

Local Dynamics: The dynamics approaching the Zone 2 steady state can be characterized analytically. Recall that the price of the new good can be written as

³¹The discussion below on the model's Zone-2 local dynamics can be omitted without loss of continuity.

$p_i = P_i(r - \delta; z_c, z_i)$. Now, assume that the economy is in Zone 2. Equation (11) holds tightly in this Zone. It gives the following difference equation for the interest rate

$$r' \beta P_i(r - \delta; z_c, z_i) = P_i(r' - \delta; z'_c, z'_i). \quad (20)$$

To have a steady state, technological progress must abate. Hence, suppose that $z'_c = z_c$, and $z'_i = z_i$. What can be said about the solution to this difference equation in this situation? The lemma below provides the answer. The cases described by the lemma are portrayed in Figure 11.

Lemma *The difference equation (20) has two rest points, viz $r = 1/\beta$ and $r = \delta$. Its local dynamics are as follows:*

1. *When $\kappa - \omega < 0$ the system converges monotonically to the rest point given by $r = 1/\beta$. The rest point $r = \delta$ is unstable.*
2. *When $\kappa - \omega > 0$ two modes of behavior can happen:*
 - (a) *If $(\kappa - \omega)/(1 - \omega) < 1 - \beta\delta$ then the system converges monotonically to the rest point $r = \delta$. The system exhibits oscillations around the $r = 1/\beta$ rest point. These cycles converge when $(\kappa - \omega)/(1 - \omega) < (1 - \beta\delta)/2$ and diverge otherwise.*
 - (b) *Alternatively, if $(\kappa - \omega)/(1 - \omega) > 1 - \beta\delta$ the system converges monotonically towards the rest point $r = \delta$. The rest point $r = 1/\beta$ is unstable.*

Proof. See Appendix ■

Remark *The calibrated version of model is described by Case 1. Suppose instead that $\kappa - \omega > 0$. Then, as a practical matter, any reasonable calibration will result in $(\kappa - \omega)/(1 - \omega) < (1 - \beta\delta)/2$. This will transpire because the differences in capital shares across industries are small. Hence, for all empirically relevant equilibrium the rest point $r = 1/\beta$ will be stable.*

Sectoral Shifts: The transitional dynamics for the model are shown in Figure 12. Given the parameterization adopted, convergence to the new steady state (where

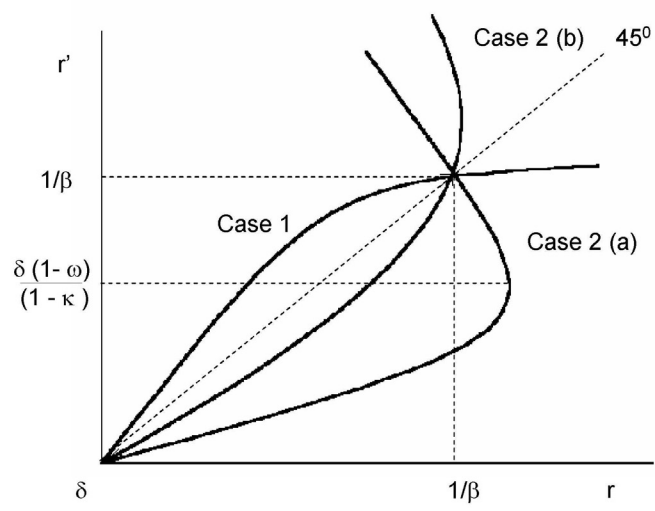


Figure 11: The Model's Local Dynamics, Zone 2.

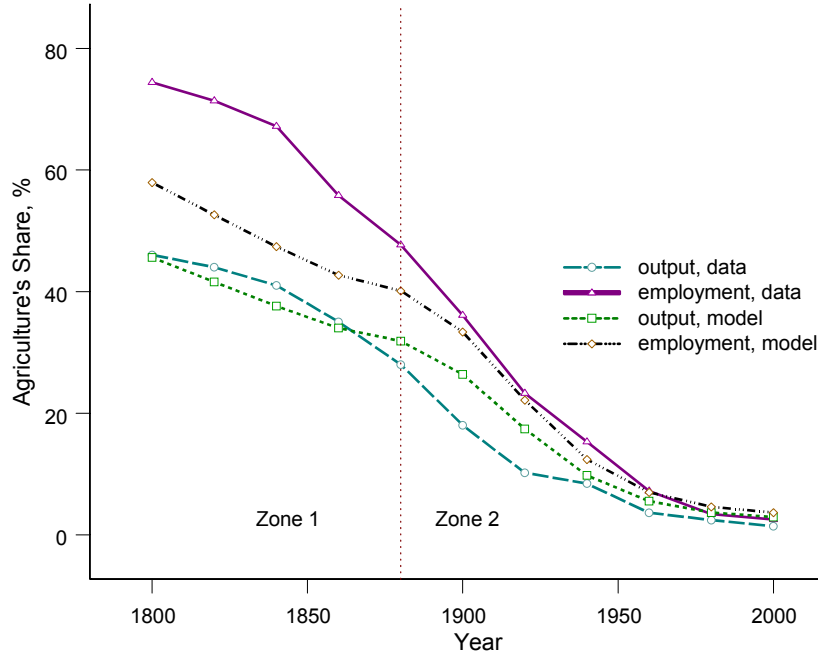


Figure 12: The Decline of Agriculture, 1800-2000 – U.S. Data and Model.

$r = 1/\beta$) is monotone. (I.e., the economy is described by Case 1 in the lemma.) The model economy transits out of Zone 1 into Zone 2 in 1880. Observe that agriculture's shares of GDP and employment decline along with technological progress. The time paths predicted by the model match the data very well, with one blemish that will be discussed now.

Note that in the U.S. data, agriculture's share of employment, ϑ , significantly exceeded its share of output, χ , in 1800. This is a bit of task to achieve with a Cobb-Douglas production structure, at least when new goods aren't produced. To see why, note that the efficiency conditions for employment in agriculture and generic manufacturing imply that the following relationship between relative employment and outputs must hold

$$\frac{\chi}{1 - \chi} \equiv \frac{p_a y_a}{y_c} = \frac{1 - \omega l_a}{1 - \lambda l_c} \equiv \frac{1 - \omega}{1 - \lambda} \frac{\vartheta}{1 - \vartheta}.$$

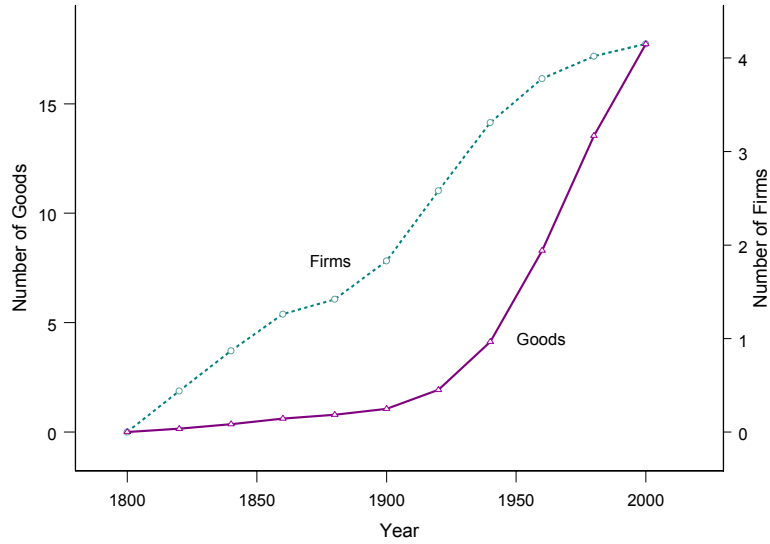


Figure 13: The Rise in the Number of New Goods and Firms, 1800-2000 – Model.

Hence, if agriculture is to constitute a higher fraction of employment vis a vis output then labor’s share of income must be disproportionately higher in this sector; i.e., $(1 - \lambda)/(1 - \omega)$ must be bigger than one since $[\vartheta/(1 - \vartheta)]/[\chi/(1 - \chi)]$ is. This could be done by picking a high value for ω , or capital’s share of income in the generic sector. The required value is 0.74. This value is unrealistic and implies that small changes in non-agricultural TFP will have enormous effects on output.

Coinciding with the fall in agriculture is the rise in new goods, as Figure 13 illustrates. As can be seen, at low levels of economic development no new goods are produced. As the state of technology progresses income rises. Workers begin to demand new goods. Both the number of new goods produced, and the number of firms producing them, rise. On some other dimensions the predictions for the model are reasonable. The interest rate is trapped between 4.6 and 8.2 percent. Labor’s share of income hovers around 70 percent.

IV. Conclusions

So, what is the connection between technological progress, the introduction of new goods, and the structure of production? A simple story is told here. As incomes rise, it pays for producers to introduce new goods and services. Consumers demand new goods as incomes rise because the benefit from consuming a new good is higher than the benefit from consuming more of an old good. The appealing aspect of this explanation is that in the data the importance of agriculture seems to fall unabated as economies develop, and the model developed here is consistent with that prediction. (More precisely, so long as TFP increases, agriculture's share of GDP keeps declining. It does not asymptote to a positive constant.)

The model developed here also provides a framework, albeit crude, with which to analyze the impact that new goods have on economic welfare. The impact of technological progress on economic welfare is sizable. The exact magnitude depends on the welfare criteria used. The analysis suggests that economic welfare grew by at least 1.5 percent a year, and by perhaps as much as 10 percent a year. More elaborate versions of the model could undoubtedly do a better job. For instance, process innovation could be incorporated into the framework to capture the decline in a product's price after its introduction. At a point in time, each vintage of new goods would then be consumed in differing amounts. Over time the consumption of a new product would follow a diffusion curve. This may create more powerful substitution effects that could create some divergence among the various indices of welfare. A model provides an ideal laboratory to evaluate the performance of the various indices.

V. Appendix

A. The Lemma

By using the first-order conditions to problem (14), it can be deduced that the profits earned by a firm in the new goods sector will be given by

$$\pi_i = (1 - \kappa - \tau)\kappa^{\kappa/(1-\kappa-\tau)}\tau^{\tau/(1-\kappa-\tau)}(p_i z_i)^{1/(1-\kappa-\tau)}(r - \delta)^{-\kappa/(1-\kappa-\tau)}w^{-\tau/(1-\kappa-\tau)} - w\phi = 0.$$

Next, the first-order conditions to problem (12) imply that

$$w = W(r - \delta; z_c) \equiv (1 - \omega)z_c \left(\frac{r - \delta}{\omega z_c}\right)^{\omega/(\omega-1)}. \quad (21)$$

Using the above two equations in conjunction with (15) allows the price for new goods to be written as

$$p_i = P_i(r - \delta; z_c, z_i) \equiv z_i^{-1} \left[\frac{\phi}{(1 - \kappa - \tau)} \right]^{(1-\kappa-\tau)} \kappa^{-\kappa} \tau^{-\tau} \times (1 - \omega)^{1-\kappa} \omega^{(1-\kappa)\omega/(1-\omega)} z_c^{(1-\kappa)/(1-\omega)} (r - \delta)^{[\kappa-\omega]/(1-\omega)}. \quad (22)$$

It is then straightforward to calculate that

$$P_{i1}(r - \delta; z_c, z_i) = \frac{1}{r - \delta} \frac{\kappa - \omega}{(1 - \omega)} P_i(r - \delta; z_c, z_i). \quad (23)$$

With (22) in hand, it is easy to see that the difference equation (20) can be rewritten as

$$r' \beta (r - \delta)^{[\kappa-\omega]/(1-\omega)} = (r' - \delta)^{[\kappa-\omega]/(1-\omega)}, \quad (24)$$

when $z'_c = z_c$ and $z'_i = z_i$. What can be said about the solutions to this equation?

Lemma *The difference equation (20) has two rest points, viz $r = 1/\beta$ and $r = \delta$. Its local dynamics are as follows:*

1. When $\kappa - \omega < 0$ the system converges monotonically to the rest point given by $r = 1/\beta$. The rest point $r = \delta$ is unstable.

2. When $\kappa - \omega > 0$ two modes of behavior can happen:

- (a) If $(\kappa - \omega)/(1 - \omega) < 1 - \beta\delta$ then the system converges monotonically to the rest point $r = \delta$. The system exhibits oscillations around the $r = 1/\beta$ rest point. These cycles converge when $(\kappa - \omega)/(1 - \omega) < (1 - \beta\delta)/2$ and diverge otherwise.
- (b) Alternatively, if $(\kappa - \omega)/(1 - \omega) > 1 - \beta\delta$ the system converges monotonically towards the rest point $r = \delta$. The rest point $r = 1/\beta$ is unstable.

Proof. Rewrite the mapping given by (20) as

$$r' = D(r; z_c, z_i). \quad (25)$$

(Recall that in a steady state, $z'_c = z_c$ and $z'_i = z_i$.) It's clear from (24) that $r' = r = 1/\beta$ and $r' = r = \delta$ are both rest points to this equation. By the implicit function theorem D is a C^1 function with

$$\frac{dr'}{dr} = D_1(r; z_c, z_i) = \frac{r' \beta P_{i1}(r - \delta; z_c, z_i)}{P_{i1}(r' - \delta; z_c, z_i) - \beta P_i(r - \delta; z_c, z_i)}. \quad (26)$$

Using (22), (23), and (20) in (26) it can be calculated that

$$\begin{aligned} \frac{dr'}{dr} &= D_1(r; z_c, z_i) = \frac{[(\kappa - \omega)/(1 - \omega)]r'(r'\beta)^{(1-\omega)/(\kappa-\omega)}}{[(\kappa - \omega)/(1 - \omega)]r' - (r' - \delta)} \\ &= \frac{[(\kappa - \omega)/(1 - \omega)]r'(r'\beta)^{(1-\omega)/(\kappa-\omega)}}{\Delta(r')}. \end{aligned} \quad (27)$$

First, if $\kappa - \omega < 0$ then $P_{i1}(r - \delta; z_c, z_i)$ and $P_{i1}(r' - \delta; z_c, z_i) < 0$. From (26) it is easy to see that $dr'/dr = D_1(r; z_c, z_i) > 0$ for all r and r' combinations. Therefore, the law of motion D rises continuously from the point $r' = r = \delta$ and converges asymptotically to $\lim_{r \rightarrow \infty} D(r; z_c, z_i) = \infty$. It is also easy to deduce that $dr'/dr|_{r'=r=1/\beta} = D_1(1/\beta; z_c, z_i) < 1$; in fact, $D_1(r; z_c, z_i) < 1$ whenever $r > 1/\beta$. Furthermore, from (27) it can be seen that $dr'/dr|_{r'=r=\delta} = D_1(\delta; z_c, z_i) = (\delta\beta)^{(1-\omega)/(\kappa-\omega)} > 1$. Hence, the system converges monotonically to the rest point $r' = r = 1/\beta$ from any $r \neq \delta$.

Second, suppose that $\kappa - \omega > 0$. From (27) it is apparent that

$$\frac{dr'}{dr} \begin{matrix} \geq \\ \leq \end{matrix} 0 \text{ as } \Delta(r') \begin{matrix} \geq \\ \leq \end{matrix} 0.$$

In turn it is easy to compute that

$$\Delta(r') \begin{matrix} \geq \\ \leq \end{matrix} 0 \text{ as } r' \begin{matrix} \leq \\ \geq \end{matrix} \delta \left(\frac{1-\omega}{1-\kappa} \right).$$

[Note that $(1-\omega)/(1-\kappa) > 1$ when $\kappa - \omega > 0$.] Consequently, the law of motion D approaches the point $r' = \delta \left(\frac{1-\omega}{1-\kappa} \right) \equiv \xi$ and $r = (\xi - \delta)/(\xi\beta)^{(1-\omega)/(\kappa-\omega)} + \delta$ from two ways: (i) upwards from below, and (ii) downwards from above. That is, it starts off from $r' = r = \delta$ and rises upwards to $r' = \delta \left(\frac{1-\omega}{1-\kappa} \right) \equiv \xi$ and $r = (\xi - \delta)/(\xi\beta)^{(1-\omega)/(\kappa-\omega)} + \delta$. It then bends backwards, and as r returns to δ , the law of motion D asymptotes to $\lim_{r \rightarrow \delta} D(r; z_c, z_i) = \infty$. Now, from (27) it is obvious that $0 < dr'/dr|_{r'=r=\delta} = D_1(\delta; z_c, z_i) = (\delta\beta)^{(1-\omega)/(\kappa-\omega)} < 1$. Therefore, the rest point $r' = r = \delta$ is locally stable.

What about the other rest point, $r' = r = 1/\beta$? Two subcases occur depending on whether $\Delta(1/\beta) \begin{matrix} \geq \\ \leq \end{matrix} 0$. First, note that

$$\Delta(1/\beta) \begin{matrix} \geq \\ \leq \end{matrix} 0 \text{ as } \frac{\kappa - \omega}{1 - \omega} \begin{matrix} \geq \\ \leq \end{matrix} 1 - \beta\delta.$$

Now assume that $\Delta(1/\beta) > 0$. It follows from (27) that $dr'/dr|_{r'=r=1/\beta} > 1$. In this case the rest point $r' = r = 1/\beta$ is unstable. Alternatively, suppose that $\Delta(1/\beta) < 0$. Here, the system oscillates around the rest point $r' = r = 1/\beta$. Are these oscillations locally stable? Equation (27) implies that

$$dr'/dr|_{r'=r=1/\beta} \begin{matrix} \geq \\ \leq \end{matrix} -1 \text{ as } \frac{\kappa - \omega}{1 - \omega} \begin{matrix} \leq \\ \geq \end{matrix} (1 - \beta\delta)/2.$$

■

B. Transitional Dynamics

Pick a T large enough so that convergence takes place within $T + 1$ periods. That is, so that all variables in the model will take their steady state values by period

$T + 1$. Start iteration j with a guess for the interest rate path, $\{r_t\}_{t=0}^T$, and the time path for the number of new goods consumed by the young, $\{I_t\}_{t=0}^T$, denoted by $\{r_t^j\}_{t=0}^T$ and $\{I_t^j\}_{t=0}^T$ respectively. Now, with a little bit of work, it can be shown that

$$p_a = P_a(r - \delta; z_a, z_c) \equiv \frac{(r - \delta)^\lambda w^{1-\lambda}}{z_a \lambda^\lambda (1 - \lambda)^{(1-\lambda)}}. \quad (28)$$

Hence, a guess can be obtained, using (28), (22) and (21), for the price and wage paths $\{p_{a,t}\}_{t=0}^T, \{p_{i,t}\}_{t=0}^T$, and $\{w_t\}_{t=0}^T$. Represent this by $\{p_{a,t}^j\}_{t=0}^T, \{p_{i,t}^j\}_{t=0}^T$, and $\{w_t^j\}_{t=0}^T$.

Time period t : In time period t the state variables will be k_t, b_t , and r_t . Given the guess $\{r_{x+1}^j\}_{x=t+1}^T$ and $\{I_x^j\}_{x=t+1}^T$, a solution for either r_{t+1} or I_t must be found, depending on whether the model is in Zone 1 or Zone 2. This is done using the capital market-clearing condition.

$$\mathbf{k}_{t+1} = b_{t+1}.$$

The supply of capital, b_{t+1} , derives from the optimization problem (3) for the period- t young. It is equal to their savings so that

$$b_{t+1} = w_t - c_t - p_{a,t} a_t - I_t p_{i,t} e_{\underline{s}}.$$

The demand for capital, \mathbf{k}_{t+1} , reads

$$\mathbf{k}_{t+1} = k_{a,t+1} + k_{c,t+1} + \max\{I_{t+1}, I_{t+1}^o\} n_{i,t+1} k_{i,t+1}.$$

In the above equation the superscript o denotes an allocation by an old agent. Furthermore I_{t+1} is determined by the time- $(t+1)$ solution to (3) while I_{t+1}^o is determined by the time- t solution to (3) – the solutions will depend upon what zone the model is in. The period- $(t+1)$ number of firms in the new goods sector i , $n_{i,t+1}$, is given by

$$n_{i,t+1} = \left[\frac{(I_{t+1} + I_{t+1}^o) / \max\{I_{t+1}, I_{t+1}^o\}}{z_{i,t+1} k_{i,t+1}^\kappa l_{i,t+1}^\tau} \right] e_{\underline{s}}.$$

The demand for capital in the agricultural sector is given by

$$k_{a,t+1} = \frac{\mathbf{a}_{t+1}}{z_{a,t+1} (k_{a,t+1} / l_{a,t+1})^{\lambda-1}},$$

where

$$\mathbf{a}_{t+1} = a_{t+1} + a_{t+1}^o.$$

Note that a_{t+1} will be determined by the time- $(t+1)$ solution to (3) while a_{t+1}^o will obtain from the time- t solution to this problem. In the model all period- $(t+1)$ capital-labor ratios, such as $k_{a,t+1}/l_{a,t+1}$, can be expressed as functions of the period- $(t+1)$ interest rate, r_{t+1} – recall that w_{t+1} is a function of r_{t+1} . In a similar vein the capital stock employed in the new goods sector is

$$k_{i,t+1} = \left[\frac{\mathbf{s}_{i,t+1}}{z_{i,t+1}(k_{i,t+1}/l_{i,t+1})^{-\tau}} \right]^{1/(\kappa+\tau)},$$

where

$$\mathbf{s}_{i,t+1} = \frac{I_{t+1}}{\max\{I_{t+1}, I_{t+1}^o\}} e_{\mathcal{S}} + \frac{I_{t+1}^o}{\max\{I_{t+1}, I_{t+1}^o\}} e_{\mathcal{S}}.$$

Again, note that $k_{i,t+1}/l_{i,t+1}$ can be written as a function of r_{t+1} .

The period- $(t+1)$ market-clearing condition for generic manufacturing goods is

$$\mathbf{c}_{t+1} + \mathbf{k}_{t+2} - \delta \mathbf{k}_{t+1} = z_{c,t+1} k_{c,t+1} (k_{c,t+1}/l_{c,t+1})^{\omega-1},$$

which implies that

$$k_{c,t+1} = \frac{\{\mathbf{c}_{t+1} + \mathbf{k}_{t+2} - \delta[k_{a,t+1} + n_{i,t+1} \max\{I_{t+1}, I_{t+1}^o\} k_{i,t+1}]\}}{[z_{c,t+1}(k_{c,t+1}/l_{c,t+1})^{\omega-1} + \delta]}.$$

Here aggregate manufacturing consumption, \mathbf{c}_{t+1} , is

$$\mathbf{c}_{t+1} = c_{t+1} + c_{t+1}^o,$$

where c_{t+1} and c_{t+1}^o are given by the time- $(t+1)$ and time- t solutions to (3). Note that \mathbf{k}_{t+2} can readily be computed from time- $(t+1)$ aggregate savings.

By tracing through the above equations, it can be seen that, given a guess for $\{r_{x+1}^j\}_{x=t+1}^T$ and $\{I_x^j\}_{x=t+1}^T$, everything can be solved out for in terms of just either r_{t+1} or I_t depending upon whether the model is in Zone 1 or Zone 2. When the model is in Zone 2 then r_{t+1} is pinned down by the difference equation $p_{i,t+1}/r_{t+1} = \beta p_{i,t}$.

[Note that the period- t young agent's intertemporal budget constraint (4) implies that solving out for I_t is the same thing as solving out for I_{t+1}^o .³² The variable I_{t+1} comes from the guess path.] When the model is in Zone 1 then I_t (or equivalently I_{t+1}^o) is determined by the solution to the optimization problem (3) as a function of r_{t+1} .³³

Initial Period 0: At time zero there is an unanticipated wealth redistribution given the unexpected shift in technology. Hence, the initial interest rate, r_0 , that clears the capital market must also be computed. There are now two variables that need to be solved for: r_0 , and either r_1 or I_0 . That is, the initial interest rate is not a state variable that has been determined in the previous period. The solution for either r_1 or I_0 obtains in the manner described above. The solution for r_0 is achieved by adding the time-0 capital market-clearing condition

$$k_{a,0} + k_{c,0} + \max\{I_0, I_0^o\}n_{i,0}k_{i,0} = \mathbf{k}_0.$$

The demand for capital in the agricultural sector is given by

$$k_{a,0} = \frac{\mathbf{a}_0}{z_{a,0}(k_{a,0}/l_{a,0})^{\lambda-1}},$$

where

$$\mathbf{a}_0 = a_0 + a_0^o.$$

Here the solution for a_0^o obtains from

$$a_0^o = \frac{\alpha}{\alpha + \psi + \sigma I_0^o} r \mathbf{k}_0 / p_{a,0}.$$

³²It is easy to calculate that in Zone 2

$$I_{t+1}^o = w_t / (\beta p_{i,t} e \underline{s}) - (\alpha + \psi + \beta \alpha + \beta \psi) / (\sigma \beta) - I_t / \beta.$$

³³In line with (11), when $p_{i,t} < p_{i,t+1} / (r_{t+1} \beta)$ it transpires that $I_{t+1}^o = 0$. When $p_{i,t} > p_{i,t+1} / (r_{t+1} \beta)$ then

$$I_{t+1}^o = w_t r_{t+1} / (p_{i,t+1} e \underline{s}) - (\alpha + \psi + \beta \alpha + \beta \psi) / (\beta \sigma).$$

In a similar vein the capital stock employed in the new goods sector is

$$\max\{I_0, I_0^o\}n_{i,0}k_{i,0} = \max\{I_0, I_0^o\}n_{i,0}\left(\frac{(r_0 - \delta)}{\kappa p_{i,0} z_{i,0} (k_{i,0}/l_{i,0})^{-\tau}}\right)^{1/(\kappa+\tau-1)}.$$

In the above two equations I_0 is determined by the time-0 solution to (3) while I_0^o will be specified by

$$I_0^o = \max\left\{\frac{r_0 \mathbf{k}_0}{p_{i,0} e_{\underline{x}}} - \frac{\alpha + \psi}{\sigma}, 0\right\}.$$

The market-clearing condition for generic manufacturing goods is

$$\mathbf{c}_0 + \mathbf{k}_1 - \delta \mathbf{k}_0 = z_{c,0} k_{c,0} (k_{c,0}/l_{c,0})^{\omega-1},$$

which implies that

$$k_{c,0} = \{\mathbf{c}_0 + \mathbf{k}_1 - \delta \mathbf{k}_0\} / [z_{c,0} (k_{c,0}/l_{c,0})^{\omega-1}].$$

Here aggregate manufacturing consumption, \mathbf{c}_0 , is given by

$$\mathbf{c}_0 = c_0 + c_0^o,$$

where c_0 derives from (3) while c_0^o is determined by

$$c_0^o = \frac{\psi}{\alpha + \psi + \sigma I_0^o} r_0 \mathbf{k}_0.$$

The algorithm: The algorithm proceeds by iterating down the time path starting at time 0 and moving on to time period T . The solution $\{r_t, I_t\}_{t=0}^T$ obtained at each iteration j is used as a revised guess for iteration $j + 1$. The algorithm continues until $\{r_t^j, I_t^j\}_{t=0}^T \rightarrow \{r_t^{j+1}, I_t^{j+1}\}_{t=0}^T$.

VI. Research Bibliography

- ¹**Atack, Jeremy; Bateman, Fred and William N. Parker.** "The Farm, the Farmer and the Market" in Stanley Engerman and Robert E. Gallman, eds., *The Cambridge Economic History of the United States*. Cambridge: Cambridge University Press, 2000, 2, pp. 245-284.
- ²**Echevarria, Cristina.** "Changes in Sectoral Composition Associated with Economic Growth." *International Economic Review*, May 1997, 38(2), pp. 431-452.
- ³**Federal Reserve Bank of Dallas.** "The Right Stuff: America's Move to Mass Customization" in 1998 Annual Report.
- ⁴**Gallman, Robert E.** "Economic Growth and Structural Change in the Long Nineteenth Century" in Stanley Engerman and Robert E. Gallman, eds., *The Cambridge Economic History of the United States*. Cambridge: Cambridge University Press, 2000, 2, pp. 1-55.
- ⁵**Gollin, Douglas; Parente, Stephen and Richard Rogerson.** "The Role of Agriculture in Development." *American Economic Review*, May 2002, 92(2), pp. 160-164.
- ⁶**Hicks, John R.** "The Valuation of the Social Income." *Economica*, May 1940, 7(26), pp. 105-124.
- ⁷**Kongsamut, Piyabha; Rebelo, Sergio and Danyang Xie.** "Beyond Balanced Growth." *Review of Economic Studies*, October 2001, 68(4), pp. 869-882.
- ⁸**Kuznets, Simon.** "Quantitative Aspects of the Economic Growth of Nations II: Industrial Distribution of National Product and Labor Force." *Economic Development and Cultural Change*, July 1957, V(4, supplement), pp. 3-111.
- ⁹**Laitner, John.** "Structural Change and Economic Growth." *Review of Economic Studies*, July 2000, 67(3), pp. 545-561.

- ¹⁰**Lebergott, Stanley.** *Manpower in Economic Growth: The American Record since 1800.* New York: McGraw-Hill Book Company, 1964.
- ¹¹**Lebergott, Stanley.** *The American Economy: Income, Wealth and Want.* Princeton: Princeton University Press, 1976.
- ¹²**Lebergott, Stanley.** *Pursuing Happiness: American Consumers in the Twentieth Century.* Princeton, NJ: Princeton University Press, 1993.
- ¹³**Lebergott, Stanley.** *Consumer Expenditures: New Measures and Old Motives.* Princeton, NJ: Princeton University Press, 1996.
- ¹⁴**Margo, Robert A.** "The Labor Force in the Nineteenth Century" in Stanley Engerman and Robert E. Gallman, eds., *The Cambridge Economic History of the United States.* Cambridge: Cambridge University Press, 2000, 2, pp. 207-243.
- ¹⁵**Mitchell, Brian R.** *International Historical Statistics: The Americas, 1750-1993.* New York, N.Y.: Stockton Press, 1998.
- ¹⁶**Rogerson, Richard.** "Indivisible Labor, Lotteries and Equilibrium." *Journal of Monetary Economics*, January 1988, 21(3), pp. 3-16.
- ¹⁷**Romer, Paul M.** "Growth Based on Increasing Returns Due to Specialization." *American Economic Review*, May 1987, 77(2), pp. 56-62.
- ¹⁸**U.S. Bureau of the Census.** *Historical Statistics of the United States: Colonial Times to 1970.* Washington, D.C.: U.S. Bureau of the Census, 1975.
- ¹⁹**Weiss, Thomas.** "Economic Growth before 1860: Revised Conjectures" in Thomas Weiss and Donald Schaefer, eds., *American Economic Development in Historical Perspective.* Stanford: Stanford University Press, 1994, 11-27.
- ²⁰**Williamson, Jeffrey G.** "The Evolution of Global Labor Markets Since 1830: Background Evidence and Hypotheses." *Explorations in Economic History*, April 1995, 32(2), pp. 141-196.

²¹**Yorukoglu, Mehmet.** “Product vs. Process Innovations and Economic Fluctuations.” *Carnegie-Rochester Conference Series on Public Policy*, June 2000, 52, pp. 137-163.